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Minkoff

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[54] **INTERFERENCE REJECTION BY MEANS OF NULL-SPACE TRANSFORMATIONS**

[75] Inventor: **John Minkoff**, Englewood, N.J.

[73] Assignee: **Lucent Technologies, Inc.**, Murray Hill, N.J.

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[51] **Int. Cl.**[7] **H04Q 7/32**

[52] **U.S. Cl.** **455/561**; 455/562; 342/357.08; 342/357.12

[58] **Field of Search** 455/62, 63, 67.1, 455/67.3, 67.6, 450, 452, 561, 562, 161, 272, 73, 132, 277.1; 342/357, 357.12, 360, 423

[56] **References Cited**

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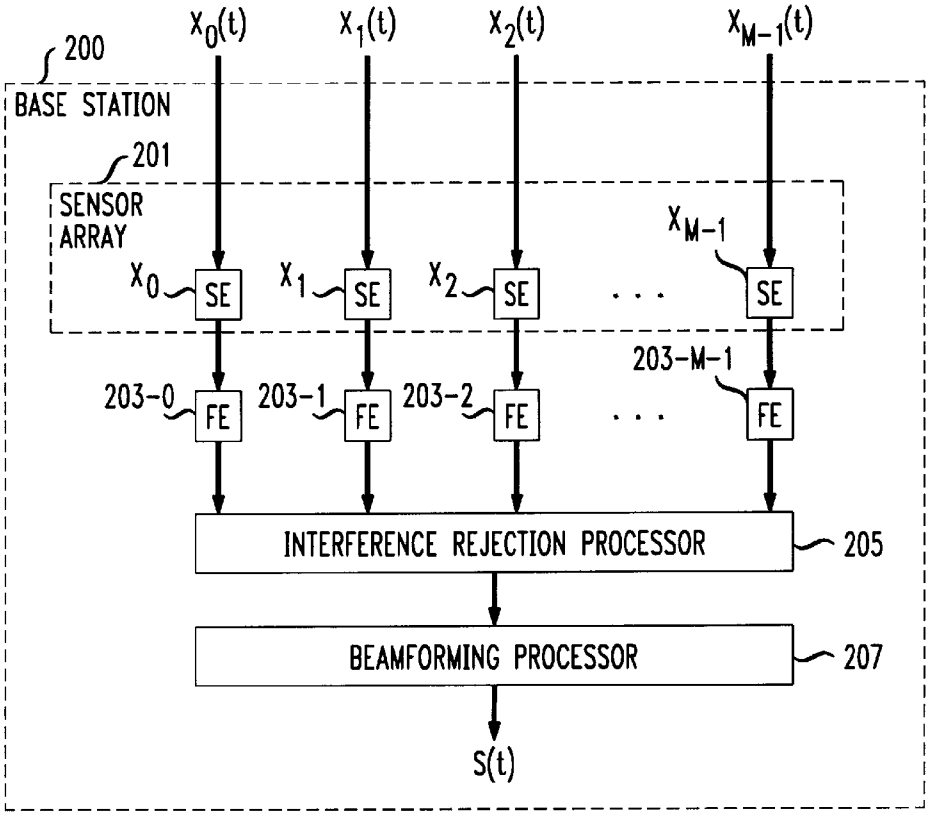
Primary Examiner—Wellington Chin
Assistant Examiner—Pablo Tran

[57] **ABSTRACT**

A technique for interference rejection at a sensor array is disclosed that employs a transformation on the output of the sensor array wherein the angular location of the source of each interfering signal constitutes the null-space of the transformation. For a sensor array of M sensor elements, the rejection of up to M−1 interferers is possible with a single transformation. One embodiment of the present invention comprises: receiving M signals, $x_0(t)$ through $x_{M-1}(t)$, at a frequency of ω radians/second at a sensor array comprising M spatially-disparate sensor elements, x_0 through x_{M-1}, wherein the M signals, $x_0(t)$ through $x_{M-1}(t)$, comprise a signal of interest incident on the sensor array at an angle ϕ, and an interfering signal incident on the sensor array at an angle ψ_1; transforming each of the M signals, $x_0(t)$ through $x_{M-1}(t)$, by a first factor based on ω, ψ_1, the speed of propagation of the interfering signal, and the distance between the sensor elements, x_0 through x_{M-1}, to form M intermediate products $s'_1(t)$ through $s'_{M-1}(t)$; and transforming each of the M intermediate products $s'_1(t)$ through $s'_{M-1}(t)$ by a second factor based on ω, Φ, ψ_1, the speed of propagation of the interfering signal, and the distance between the sensor elements, x_0 through x_{M-1}, to form M signals $s_1(t)$ through $s_{M-1}(t)$.

13 Claims, 3 Drawing Sheets



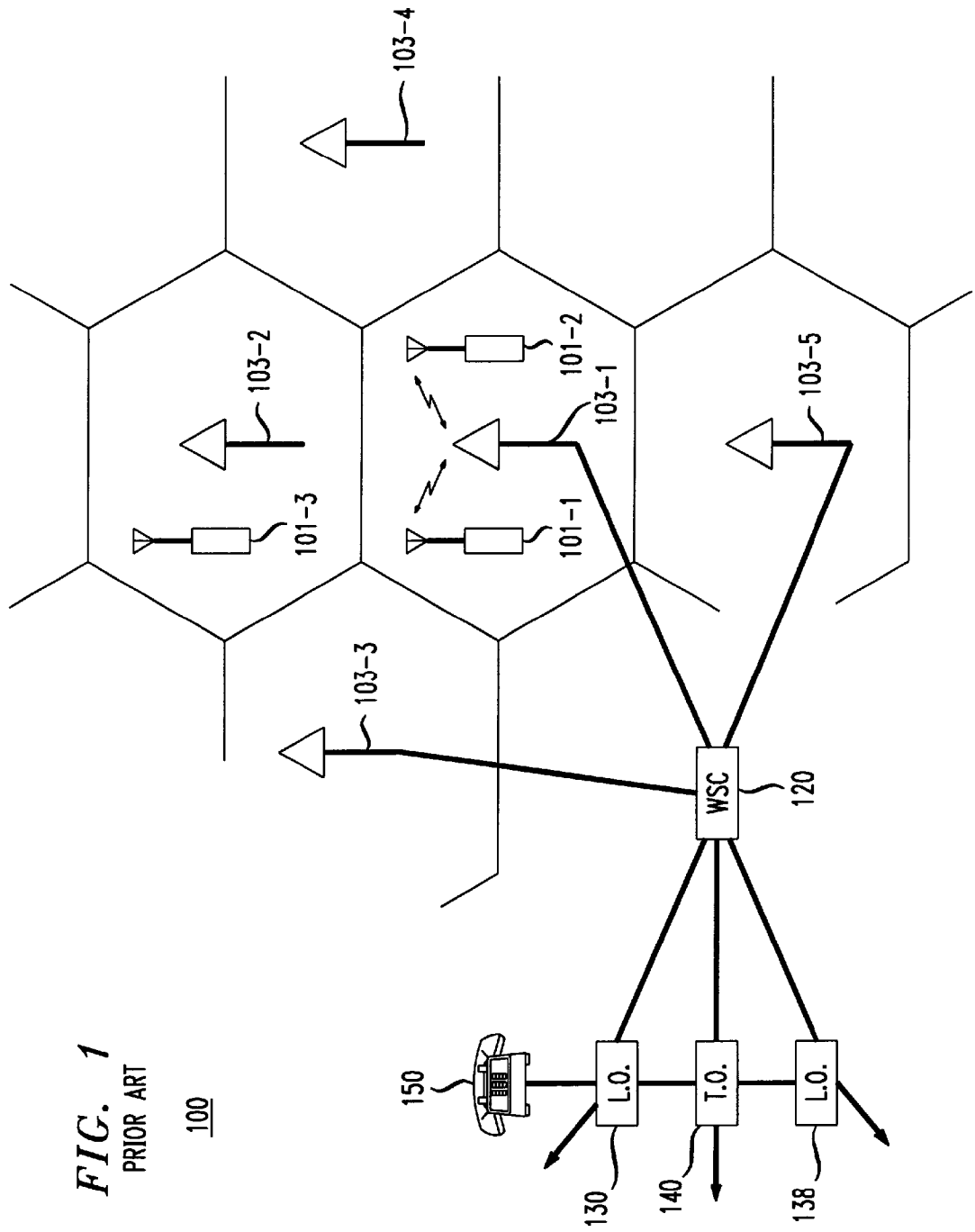


FIG. 1
PRIOR ART

100

FIG. 2

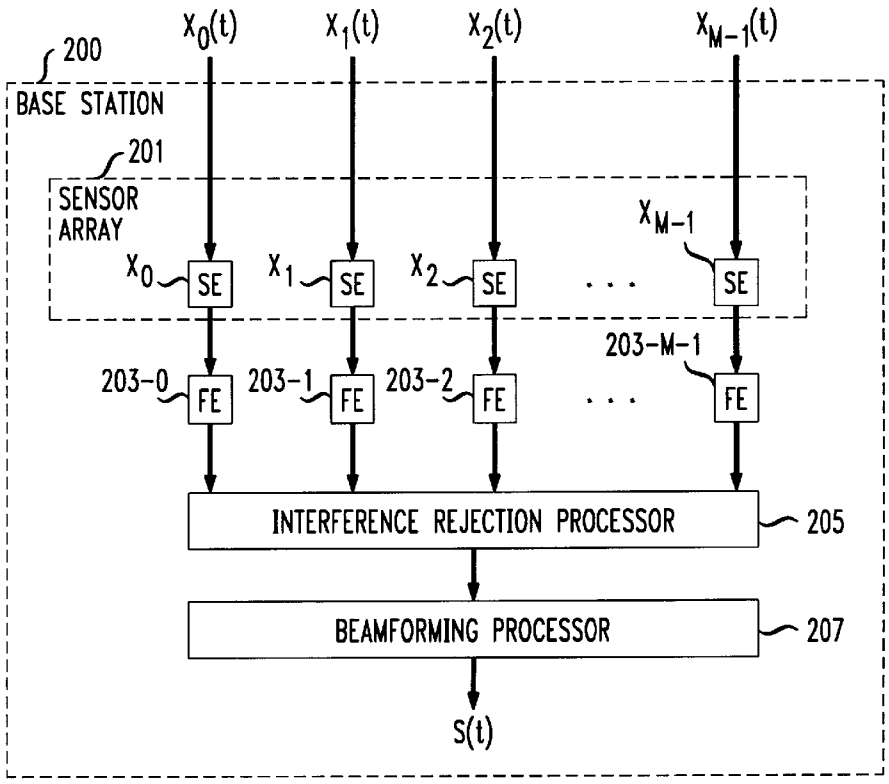

$X_0(t)$
$X_1(t)$
$X_2(t)$
$X_{M-1}(t)$
200
BASE STATION
201
SENSOR ARRAY
X_0
X_1
X_2
X_{M-1}
SE
203-0
203-1
203-2
203-M-1
FE
INTERFERENCE REJECTION PROCESSOR
205
BEAMFORMING PROCESSOR
207
S(t)

FIG. 3

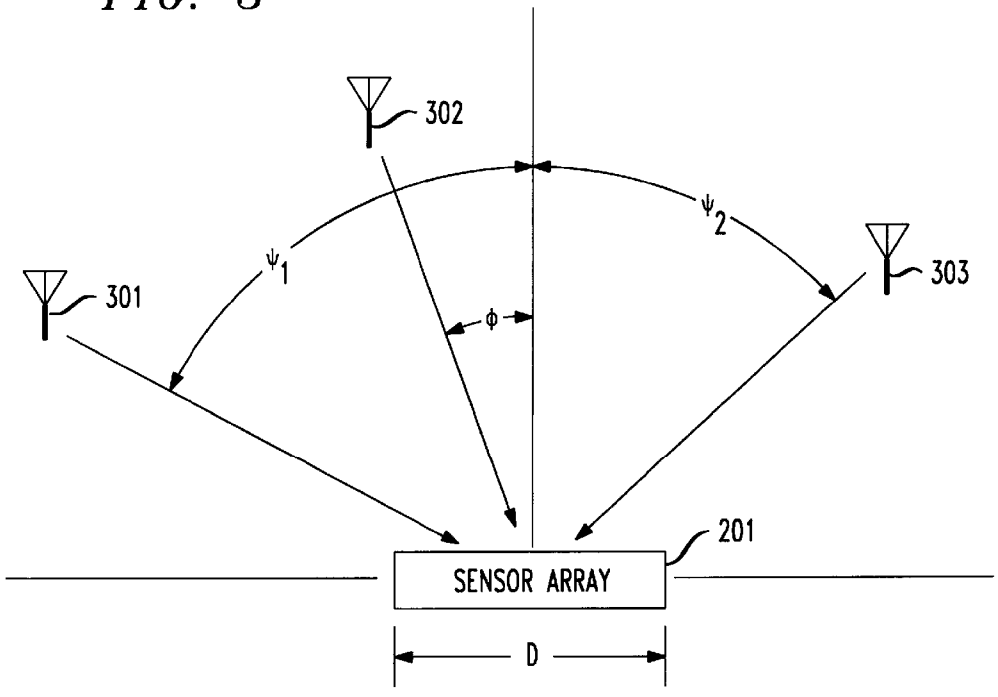
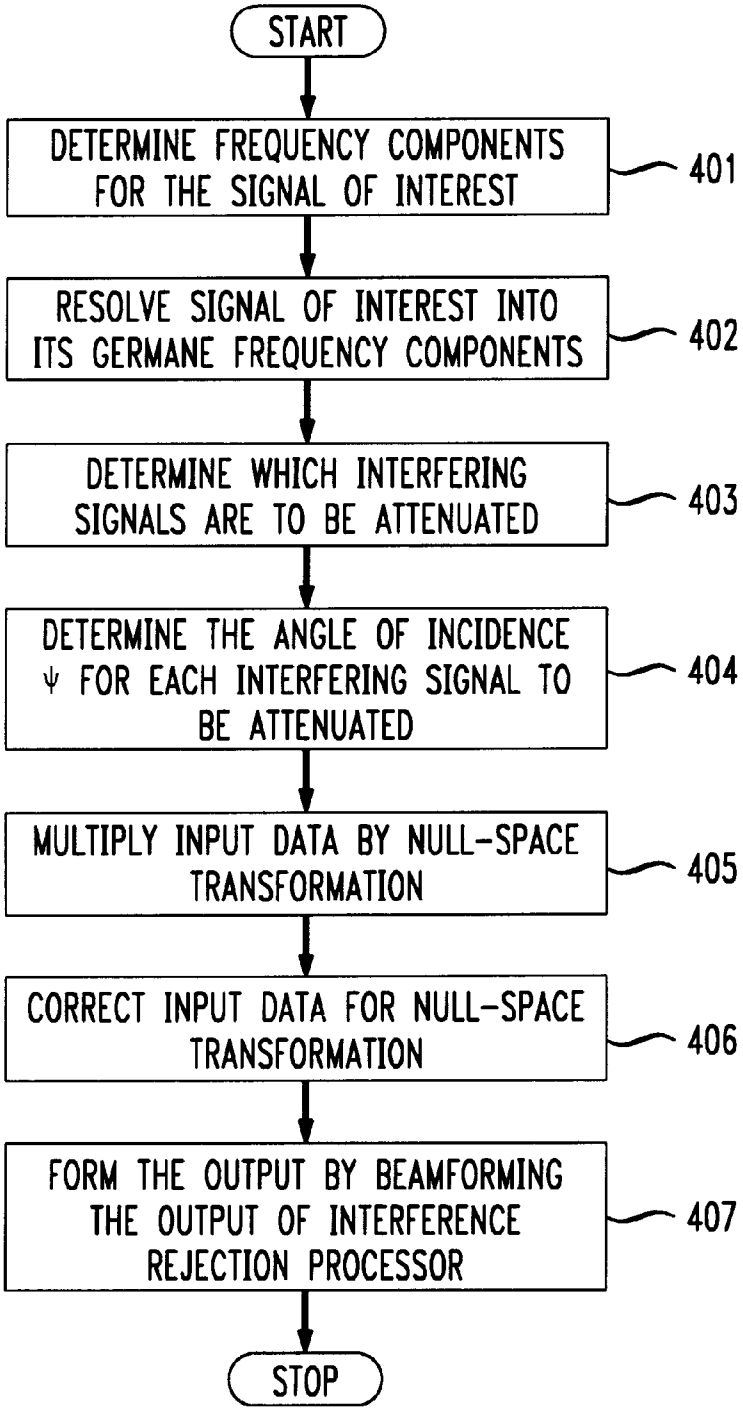

302
301
303
ψ_1
ψ_2
ϕ
201
SENSOR ARRAY
D

FIG. 4


START
DETERMINE FREQUENCY COMPONENTS FOR THE SIGNAL OF INTEREST
401
RESOLVE SIGNAL OF INTEREST INTO ITS GERMANE FREQUENCY COMPONENTS
402
DETERMINE WHICH INTERFERING SIGNALS ARE TO BE ATTENUATED
403
DETERMINE THE ANGLE OF INCIDENCE ψ FOR EACH INTERFERING SIGNAL TO BE ATTENUATED
404
MULTIPLY INPUT DATA BY NULL-SPACE TRANSFORMATION
405
CORRECT INPUT DATA FOR NULL-SPACE TRANSFORMATION
406
FORM THE OUTPUT BY BEAMFORMING THE OUTPUT OF INTERFERENCE REJECTION PROCESSOR
407
STOP

INTERFERENCE REJECTION BY MEANS OF NULL-SPACE TRANSFORMATIONS

FIELD OF THE INVENTION

The present invention relates to sensor arrays (e.g., sonar arrays, antenna arrays, etc.) in general, and, more particularly, to a technique for mitigating the effect of interfering signals at a sensor array.

BACKGROUND OF THE INVENTION

FIG. **1** depicts a schematic diagram of a portion of a typical wireless telecommunications system, which provides wireless telecommunications service to a number of wireless terminals (e.g., wireless terminals **101-1** through **101-3**) that are situated within a geographic region. The heart of a typical wireless telecommunications system is Wireless Switching Center ("WSC") **120**, which might be also known as a Mobile Switching Center ("MSC") or Mobile Telephone Switching Office ("MTSO"). Typically, Wireless Switching Center **120** is connected to a plurality of base stations (e.g., base stations **103-1** through **103-5**) that are dispersed throughout the geographic area serviced by the system and to the local- and long-distance telephone offices (e.g., local-office **120**, local-office **138** and toll-office **140**). Wireless Switching Center **120** is responsible for, among other things, establishing and maintaining calls between wireless terminals and between a wireless terminal and a wireline terminal, which wireline terminal is connected to Wireless Switching Center **120** via the local and/or long-distance networks.

The geographic area serviced by a wireless telecommunications system is divided into spatially distinct areas called "cells." As depicted in FIG. **1**, each cell is schematically represented by a hexagon; in practice, however, each cell has an irregular shape that depends on the topography of the terrain surrounding the cell. Typically, each cell contains a base station, which comprises the radios and antennas that the base station uses to communicate with the wireless terminals in that cell and also comprises the transmission equipment that the base station uses to communicate with Wireless Switching Center **120**.

For example, when wireless terminal **101-1** desires to communicate with wireless terminal **101-2**, wireless terminal **101-1** transmits the desired information to base station **103-1**, which relays the information to Wireless Switching Center **120**. Upon receipt of the information, and with the knowledge that it is intended for wireless terminal **101-2**, Wireless Switching Center **120** then returns the information back to base station **103-1**, which relays the information, via radio, to wireless terminal **101-2**.

Typically, each base station receives one or more interfering signals at the same frequency as the signal of interest, which interferes with the capability of the base station to discern the signal of interest by lowering the signal-to-noise ratio of the signal of interest. Therefore, the need exists for a technique that mitigates the effect of the interfering signals.

SUMMARY OF THE INVENTION

Some embodiments of the present invention are capable of mitigating the effects of an interfering signal without some of the costs and disadvantages associated with techniques in the prior art. In particular, some embodiments of the present invention are computationally efficient and can mitigate the effects of an interfering signal that originates arbitrarily close to, in angular orientation, the source of the signal of interest. Furthermore, some embodiments of the present invention are suitable for signals of interest that employ spread spectrum modulation techniques (e.g., ID-95 CDMA, etc.).

Embodiments of the present invention advantageously employ a sensor array (e.g., an antenna array, a sonar array, etc.) comprising M sensor elements and an "open-loop" or two-step approach to interference rejection. In the first step, the angular location ψ of the source of each interfering signal whose effect is to be mitigated or "rejected" is determined. In the second step, each signal received by a sensor element in the sensor array is transformed by a matrix that is constructed such that its "null space" is based on the angular location of the source of each interfering signal. The transformation is computationally simple, requires no matrix inversions and the rejection of multiple interfering signals is no more computationally complex than the rejection of a single interfering signal. For a sensor array of M sensor elements, the illustrative embodiment of the present invention is capable of rejecting up to M−1 interfering signals with each matrix transformation. The rejection of more than M−1 interfering signals can be accomplished by additional transformations.

One embodiment of the present invention comprises: receiving M signals, $x_0(t)$ through $x_{M-1}(t)$, at a frequency of ω radians/second at a sensor array comprising M spatially-disparate sensor elements, x_0 through x_{M-1}, wherein the M signals, $x_0(t)$ through $x_{M-1}(t)$, comprise a signal of interest incident on the sensor array at an angle ϕ, and an interfering signal incident on the sensor array at an angle ψ_1; transforming each of the M signals, $x_0(t)$ through $x_{M-1}(t)$, by a first factor based on ω, ψ_1, the speed of propagation of the interfering signal, and the distance between the sensor elements, x_0 through x_{M-1}, to form M intermediate products $s'_1(t)$ through $s'_{M-1}(t)$; and transforming each of the M intermediate products $s'_1(t)$ through $s'_{M-1}(t)$ by a second factor based on ω, ϕ, ψ_1, the speed of propagation of the interfering signal, and the distance between the sensor elements, x_0 through x_{M-1}, to form M signals $s_1(t)$ through $s_{M-1}(t)$.

BRIEF DESCRIPTION OF THE DRAWINGS

FIG. **1** depicts a schematic diagram of a wireless telecommunications system in the prior art.

FIG. **2** depicts a block diagram of wireless telecommunications base station **300** in accordance with the illustrative embodiment of the present invention.

FIG. **3** depicts a map of the relative angular relationship of sensor array **201** to three illustrative signal sources.

FIG. **4** depicts a flowchart of the operation of the illustrative embodiment of the present invention.

DETAILED DESCRIPTION

FIG. **2** depicts a block diagram of wireless telecommunications base station **300** in accordance with the illustrative embodiment of the present invention. Base station **300** advantageously comprises: sensor array **201**, which comprises: M sensor elements, x_0 through x_{M-1}, M front-ends, **203-0** through **203**-M−1, interference rejection processor **205**, and beamforming processor **207**, interconnected as shown.

Sensor elements, x_0 through x_{M-1}, are advantageously evenly spaced in a line and compose sensor array **201**. It will be clear to those skilled in the art how to make and use embodiments of the present invention in which the sensor

elements, x_0 through x_{M-1}, are not equally spaced or are not arranged linearly or are neither equally spaced or linearly arranged. For the purposes of this specification, the distance from sensor element x_0 to sensor element x_n is defined as d_n.

Each sensor element, x_0 through x_{M-1}, is advantageously a conventional antenna element for receiving an electromagnetic signal. It will be clear to those skilled in the art how to make and use embodiments of the present invention in which each sensor element is a microphone element for receiving an acoustic signal.

As is well-known to those skilled in the art, each sensor element, x_0 through x_{M-1}, receives a time-varying signal, $x_0(t)$ through $x_{M-1}(t)$, respectively, in well-known fashion. Furthermore, each sensor element, x_0 through x_{M-1}, is advantageously capable of receiving the signal of interest, which can occupy either a single frequency or a range of frequencies. It will be clear to those skilled in the art how to make and use sensor array **201** and sensor elements x_0 through x_{M-1}.

Each front-end, **203-0** through **203**-M−1, receives an incoming signal from one sensor element and digitizes it, in well-known fashion, at a sample rate and with a dynamic range that is appropriate for the amplitude and frequency range of the signal of interest. It will be clear to those skilled in the art that in some embodiments of the present invention each front end advantageously comprises a low-noise amplifier for amplifying the incoming signal before it is digitized. Furthermore, it will also be clear to those skilled in the art that in some embodiments of the present invention each front end advantageously comprises a downconverter so that the digitizer can operate on intermediate frequencies. It will be clear to those skilled in the art how to make and use front-end **203-0** through **203**-M−1.

Interference rejection processor **205** and beamforming processor **207** are depicted in FIG. **2** as separate elements, for pedagogical purposes, to accentuate the difference in the function each performs. In practice, however, each can be implemented either separately or together. Advantageously, both interference rejection processor **205** and beamforming processor **207** are implemented together as an appropriately-programmed general purpose computer or digital signal processor. Alternatively, either or both of interference rejection processor **205** and beamforming processor **207** can be implemented in special-purpose hardware.

FIG. **3** depicts a map of the relative angular relationship of sensor array **201** to three illustrative signal sources: signal source **301**, signal source **302** and signal source **303**. As shown in FIG. **3**, signal source **302** radiates the signal of interest and signal sources **301** and **303** radiate interfering signals. When the frequency of the signal of interest has a wavelength of λ and a signal source is much farther than:

$$D = \frac{d^2(M-1)^2}{\lambda} \quad \text{(Eq. 1)}$$

then that signal source is in the far field of the sensor array and the signal can be considered as incident on the sensor array as a plane wave, where d is the distance between adjacent sensor elements. It will be clear to those skilled in the art how to adjust the following factors when the signal source is not in the far field of the sensor array.

In accordance with FIG. **3**, the signal of interest from signal source **302** is incident on sensor array **201** at an angle of ϕ, and the interferer from signal source **301** is incident on sensor array **201** at an angle of ψ_1, and the interferer from signal source **303** is incident on sensor array **201** at an angle of ψ_2.

FIG. **4** depicts a flowchart of the steps performed by interference rejection processor **205** and beamformer **207** in accordance with the illustrative embodiment of the present invention. Because both interference rejection processor **205** and beamforming processor **207** advantageously operate on only one frequency component of the input signal at a time, at step **401**, the frequency components of the signal of interest are determined, in well-known fashion. For example, if the signal of interest is a narrowband amplitude-modulated signal at a carrier frequency of c radians/second, then the illustrative embodiment need only be concerned with frequency components at that one frequency. Alternatively, if the signal of interest is a wideband signal (e.g., an acoustic voice signal, etc.), then the number and frequency of the frequency components of that wideband signal must be determined, and processed in steps **405**–**407** separately.

Again, because both interference rejection processor **205** and beamforming processor **207** advantageously operate on only one frequency component of the input signal at a time, at step **402**, interference rejection processor **205** advantageously resolves the signal of interest from each sensor element into its germane frequency components. As is well-known in the art, the signal of interest can be resolved into its germane frequency components using, for example, a discrete fourier transform ("DFT") on each of the input signals, $x_0(t)$ through $x_{M-1}(t)$.

Although an infinite number of interfering signals can be incident on sensor array **201**, interference rejection processor **205** is only capable of rejecting N of them, where $0 \leqq N \leqq M-1$. Therefore, at step **403**, the interfering signals to be mitigated must be determined, in well-known fashion. Advantageously, an interfering signal is identified by its angle of incidence ψ on sensor array **201**.

At step **404**, the angle of incidence ψ of each interfering signal to be mitigated must be determined. Because the illustrative embodiment is an open-loop system, the step of determining the angle of incidence ψ of each interfering signal is distinct from the step of mitigating the effect of the interfering signal. It will be clear to those skilled in the art how to determine the angle of incidence ψ of each interfering signal on the sensor array that is to be mitigated. For example, the multiple signal characterization ("MUSIC") algorithm is typical of an algorithm that determines the angle of incidence of interfering signals. See "Multiple Source DF Signal Processing: An Experimental System," R. O. Schmidt et al., IEEE Transactions on Antennas and Propagation, Vol. AP-34, No. 3, March 1986, pp. 281–290.

After the N interfering signals have been identified, and their respective angles of incidence, ψ_m, determined, for m=1 to N, then at step **405** the input to sensor array **201** is transformed by transforming the input signals, $x_0(t)$ through $x_{M-1}(t)$, by a factor, A, to form an intermediate product, S'(t):

$$S'(t)=AX(t) \quad \text{(Eq. 2)}$$

where X(t) is a column vector that equals:

$$X(t) = \begin{bmatrix} x_0(t) \\ x_1(t) \\ \vdots \\ x_{M-1}(t) \end{bmatrix} \quad \text{(Eq. 3)}$$

and A equals the matrix:

$$A = J - \sum_{m=1}^{N} v_m v_m^{\dagger} \quad \text{(Eq. 4)}$$

where J is the identity matrix of rank M, v_m is a row vector and $v_m^{\dagger}$ is the conjugate transpose of v_m. The row vector v_m is based on the angle of incidence, ψ_m, and the number of sensor elements in sensor array **201**, and is obtain from the well-known Gram-Schmidt process. *Linear Alegebra and Its Applications*. 2nd Ed., G. Strang, Academic Press, Inc., pp. 129, presents a lucid tutorial on the Gram-Schmidt process. For example:

$$v_1 = \frac{I_1}{|I_1|}, \text{ so that } |v_1|^2 = 1 \quad \text{(Eq. 5)}$$

and I_1 is a column vector based on the angle of incidence of ψ_1. I_1 equals:

$$I_1 = \begin{bmatrix} e^{i\omega\mu_{1,0}} \\ e^{i\omega\mu_{1,1}} \\ e^{i\omega\mu_{1,2}} \\ \vdots \\ e^{i\omega\mu_{1,M-1}} \end{bmatrix} \quad \text{(Eq. 6)}$$

where ω represents the frequency in radians/second of the frequency component being processed of the first interferer, and

$$\mu_{i,n} = \frac{d_n \sin\psi_i}{c} \quad \text{(Eq. 7)}$$

where d_n is the distance from sensor element x_0 to sensor element x_n, ψ_i, is the angle of incidence of interferer i on sensor array **201**, and c is the speed of propagation of interferer i as it approaches sensor array **201**.

Similarly,

$$v_2 = \frac{I_2 - (v_1, I_2)v_1}{\sqrt{|I_2|^2 + |(v_1, I_2)|^2}} \quad \text{(Eq. 8)}$$

where (A, B) is the inner product of A and B, and

$$I_i = \begin{bmatrix} e^{i\omega\mu_{i,0}} \\ e^{i\omega\mu_{i,1}} \\ e^{i\omega\mu_{i,2}} \\ \vdots \\ e^{i\omega\mu_{i,M-1}} \end{bmatrix} \quad \text{(Eq. 9)}$$

As a final example,

$$v_3 = \frac{I_3 - (v_1, I_3)v_1 - (v_2, I_3)v_2}{\sqrt{|I_3|^2 + |(v_1, I_3)|^2 + |(v_2, I_3)|^2}} \quad \text{(Eq. 10)}$$

v_i for i>3 can be obtained using the Gram-Schmidt process.

After the intermediate product S'(t) is formed in step **405**, then in step **406** each element in S'(t) must be divided by a correction factor to obtain the product S(t), which is ready for beamforming and in which the N interfering signals have been mitigated:

$$S_k(t) = \frac{S'_k(t)}{T_k} \quad \text{(Eq. 11)}$$

where

$$S'(t) = \begin{bmatrix} S'_0(t) \\ S'_1(t) \\ \vdots \\ S'_k(t) \\ \vdots \\ S'_{M-1}(t) \end{bmatrix} \quad \text{(Eq. 12)}$$

$$S(t) = \begin{bmatrix} S_0(t) \\ S_1(t) \\ \vdots \\ S_k(t) \\ \vdots \\ S_{M-1}(t) \end{bmatrix} \quad \text{(Eq. 13)}$$

and

$$T_k = 1 - \sum_{n=0}^{M-1} K_{k,n} e^{i\omega(\tau_n - \tau_k)} \quad \text{(Eq. 14)}$$

where $K_{k,e}$ is the element in the kth row and nth column of the matrix K which is obtained from:

$$K = \sum_{m=1}^{N} v_m v_m^{\dagger} \quad \text{(Eq. 15)}$$

and

$$\tau_n = \frac{d_n \sin\phi}{c} \quad \text{(Eq. 16)}$$

After the column vector S(t) has been formed, then at step **407** the process of beamforming is performed by beamforming processor **207**, which performs coherent summation of the M signals, $s_1(t)$ through $s_{M-1}(t)$, to obtain the output scalar S(t).

$$S(t)=B(\phi)S(t) \quad \text{(Eq. 17)}$$

where $B(\phi)$ is a row vector equal to:

$$B(\phi) = [\,1 \quad e^{i\omega\tau_1} \quad e^{i\omega\tau_2} \quad \cdots \quad e^{i\omega\tau_{M-1}}\,] \quad \text{(Eq. 18)}$$

It is to be understood that the above-described embodiments are merely illustrative of the invention and that many variations may be devised by those skilled in the art without departing from the scope of the invention. It is therefore intended that such variations be included within the scope of the following claims and their equivalents.

What is claimed is:

1. A method comprising:

receiving M signals, $x_0(t)$ through $x_{M-1}(t)$, at a frequency of ω radians/second at a sensor array comprising M

spatially-disparate sensor elements, x_0 through x_{M-1}, wherein said M signals, $x_0(t)$ through $x_{M-1}(t)$, comprise a signal of interest incident on said sensor array at an angle ϕ, and an interfering signal incident on said sensor array at an angle ψ_1;

transforming each of said M signals, $x_0(t)$ through $x_{M-1}(t)$, by a first factor based on ω, ψ_1, the speed of propagation of said interfering signal, and the distance between said sensor elements, x_0 through x_{M-1}, to form M intermediate products $s'_1(t)$ through $s'_{M-1}(t)$; and

transforming each of said M intermediate products $s'_1(t)$ through $s'_{M-1}(t)$ by a second factor based on ω, ϕ, ψ_1, the speed of propagation of said interfering signal, and the distance between said sensor elements, x_0 through x_{M-}, to form M signals, $s_1(t)$ through $s_{M-1}(t)$.

2. The method of claim **1** further comprising the step of beamforming by transforming each of said M signals $s_1(t)$ through $s_{M-1}(t)$ by a factor based on ω, ϕ, the speed of propagation of said interfering signal, and the distance between said sensor elements, x_0 through x_{M-1}.

3. The method of claim **1** wherein said M signals, $x_0(t)$ through $x_{M-1}(t)$, are electro-magnetic signals.

4. A wireless telecommunications base station comprising:

a sensor array for receiving M signals, $x_0(t)$ through $x_{M-1}(t)$, at a frequency of ω radians/second comprising M spatially-disparate sensor elements, x_0 through x_{M-1}, wherein said M signals, $x_0(t)$ through $x_{M-1}(t)$, comprise a signal of interest incident on said sensor array at an angle ϕ, and an interfering signal incident on said sensor array at an angle ψ_1; and

an interference rejection processor for transforming each of said M signals, $x_0(t)$ through $x_{M-1}(t)$, by a first factor based on ω, ψ_1, the speed of propagation of said interfering signal, and the distance between said sensor elements, x_0 through x_{M-1}, to form M intermediate products $s'_1(t)$ through $s'_{M-1}(t)$; and for transforming each of said M intermediate products $S'_1(t)$ through $s'_{M-1}(t)$ by a second factor based on ω, ϕ, ψ_1, the speed of propagation of said interfering signal, and the distance between said sensor elements, x_0 through x_{M-1}, to form M signals $s_1(t)$ through $s_{M-1}(t)$.

5. The wireless telecommunications base station of claim **4** further comprising a beamforming processor for beamforming by transforming each of said M signals $s_1(t)$ through $s_{M-1}(t)$ by a factor based on ω, ϕ, the speed of propagation of said interfering signal, and the distance between said sensor elements, x_0 through x_{M-1}.

6. The wireless telecommunications base station of claim **4** wherein said M signals, $x_0(t)$ through $x_{M-1}(t)$, are electromagnetic signals.

7. A method comprising:

receiving M signals, $x_0(t)$ through $x_{M-1}(t)$, at a frequency of ω radians/second at a sensor array comprising M spatially-disparate sensor elements, x_0 through x_{M-1}, wherein said M signals, $x_0(t)$ through $x_{M-1}(t)$, comprise a signal of interest incident on said sensor array at an angle ϕ, and an interfering signal incident on said sensor array at an angle ψ_1; and

transforming said plurality of signals, $x_0(t)$ through $x_{M-1}(t)$, by a matrix A to form an intermediate product S'(t), where S'(t)=AX(t), X(t) is a column vector that equals:

$$X(t) = \begin{bmatrix} x_0(t) \\ x_1(t) \\ \vdots \\ x_{M-1}(t) \end{bmatrix}$$

$$A = J - \sum_{m=1}^{N} v_m v_m^{\dagger}$$

J is the identity matrix of rank M, v_m is a row vector and $v_m^{\dagger}$ is the conjugate transpose of v_m,

$$v_1 = \frac{I_1}{|I_1|}, \text{ so that } |v_1|^2 = 1$$

$$I_1 = \begin{bmatrix} e^{i\omega\mu_{1,0}} \\ e^{i\omega\mu_{1,1}} \\ e^{i\omega\mu_{1,2}} \\ \vdots \\ e^{i\omega\mu_{1,M-1}} \end{bmatrix}$$

and

$$\mu_{i,n} = \frac{d_n \sin\psi_i}{c}$$

where d_n is the distance from sensor element x_0 to sensor element x_n, and c is the speed of propagation of interferer i as it approaches said sensor array.

8. The method of claim **7** further comprising:

transforming each of said M intermediate products $s'_1(t)$ through $s'_{M-1}(t)$ by a second factor T_k equal

$$T_k = 1 - \sum_{n=0}^{M-1} K_{k,n} e^{i\omega(\tau_n - \tau_k)}$$

where $K_{k,e}$ is the element in the kth row and nth column of the matrix K which is obtained from:

$$K = \sum_{m=1}^{N} v_m v_m^{\dagger}$$

where

$$\tau_n = \frac{d_n \sin\phi}{c}.$$

9. The method of claim **8** further comprising the step of beamforming by transforming S(t) by a factor B(ϕ), where S(t) is a column vector equal to:

$$S(t) = \begin{bmatrix} S_0(t) \\ S_1(t) \\ \vdots \\ S_k(t) \\ \vdots \\ S_{M-1}(t) \end{bmatrix}$$

and B(ϕ) is a row vector equal to:

$$B(\phi) = [\,1 \quad e^{i\omega\tau_1} \quad e^{i\omega\tau_2} \quad \cdots \quad e^{i\omega\tau_{M-1}}\,].$$

10. The method of claim **7** wherein said M signals are electro-magnetic signals.

11. A wireless telecommunications base station comprising:

a sensor array for receiving M signals, $x_0(t)$ through $x_{M-1}(t)$, at a frequency of ω radians/second comprising M spatially-disparate sensor elements, x_0 through x_{M-1}, wherein said M signals, $x_0(t)$ through $x_{M-1}(t)$, comprise a signal of interest incident on said sensor array at an angle ϕ, and an interfering signal incident on said sensor array at an angle ψ_1; and

an interference rejection processor for transforming said plurality of signals, $x_0(t)$ through $x_{M-1}(t)$, by a matrix A to form an intermediate product S'(t), where S'(t)= AX(t), X(t) is a column vector that equals:

$$X(t) = \begin{bmatrix} x_0(t) \\ x_1(t) \\ \vdots \\ x_{M-1}(t) \end{bmatrix}$$

$$A = J - \sum_{m=1}^{N} v_m v_m^{\dagger}$$

J is the identity matrix of rank M, v_m is a row vector and $v_m^{\dagger}$ is the conjugate transpose of v_m,

$$v_1 = \frac{I_1}{|I_1|}, \text{ so that } |v_1|^2 = 1$$

$$I_1 = \begin{bmatrix} e^{i\omega\mu_{1,0}} \\ e^{i\omega\mu_{1,1}} \\ e^{i\omega\mu_{1,2}} \\ \vdots \\ e^{i\omega\mu_{1,M-1}} \end{bmatrix}$$

and

$$\mu_{i,n} = \frac{d_n \sin\psi_i}{c}$$

where d_n is the distance from sensor element x_0 to sensor element x_n, and c is the speed of propagation of interferer i as it approaches said sensor array.

12. The wireless telecommunications base station of claim **11** wherein said interference rejection processor is also for transforming each of said M intermediate products $s'_1(t)$ through $s'_{M-1}(t)$ by a second factor T_k equal to:

$$T_k = 1 - \sum_{n=0}^{M-1} K_{k,n} e^{i\omega(\tau_n - \tau_k)}$$

where $K_{k,e}$ is the element in the kth row and nth column of the matrix K which is obtained from:

$$K = \sum_{m=1}^{N} v_m v_m^{\dagger}$$

$$\text{where } \tau_n = \frac{d_n \sin\phi}{c}.$$

13. The wireless telecommunications base station of claim **11** further comprising a beamforming processor for beamforming by transforming S(t) by a factor B(ϕ), where S(t) is a column vector equal to:

$$S(t) = \begin{bmatrix} S_0(t) \\ S_1(t) \\ \vdots \\ S_k(t) \\ \vdots \\ S_{M-1}(t) \end{bmatrix}$$

and B(ϕ) is a row vector equal to:

$$B(\phi) = [\,1 \quad e^{i\omega\tau_1} \quad e^{i\omega\tau_2} \quad \cdots \quad e^{i\omega\tau_{M-1}}\,].$$

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